

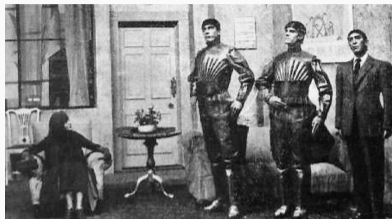
ROBOTS THAT LEARN WORLD REPRESENTATIONS, WHY AND WHICH ONES?

Stéphane Caron

March 21, 2023

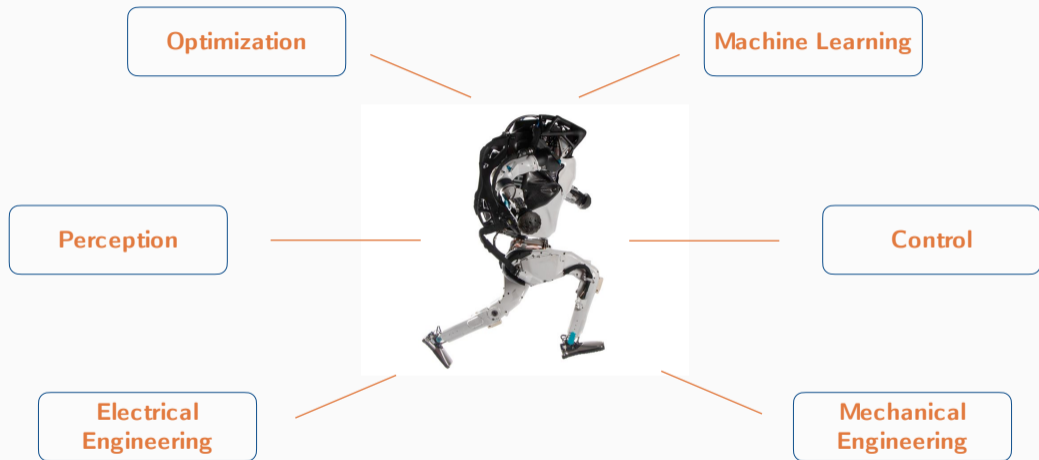
Researcher at Inria and ENS-PSL





¹Emanuel Todorov. "Goal directed dynamics". In: *IEEE International Conference on Robotics and Automation*. 2018.

ROBOTICS IS MULTIDISCIPLINARY



SOME ROBOTS



LEGGED ROBOTS IN FRANCE

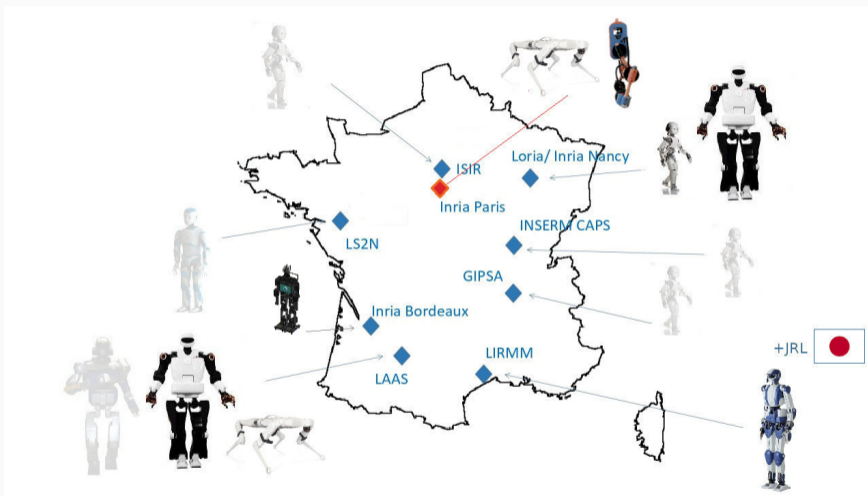


Figure 1: Research labs with legged robots (France, 2023)

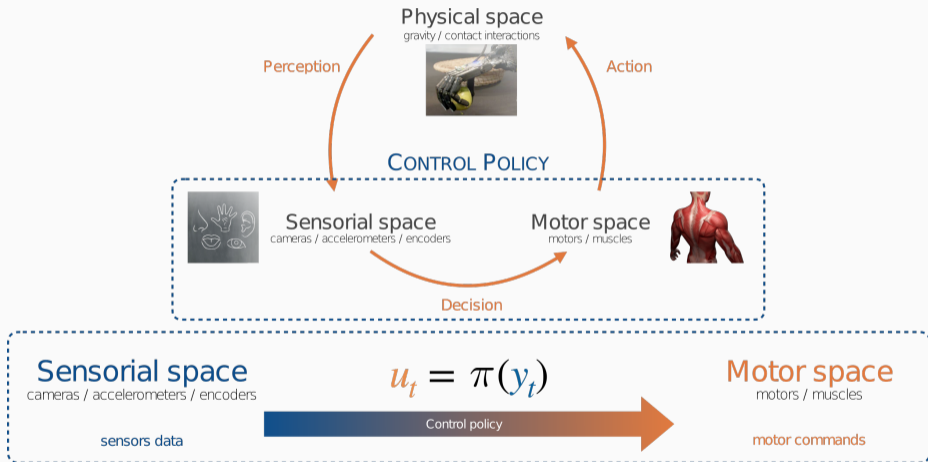
OPTIMIZATION PLAYS A KEY ROLE IN ROBOTICS



$$\begin{aligned} & \underset{x}{\text{minimize}} && f(x) \\ & \text{subject to} && g(x) = 0 \\ & && h(x) \leq 0 \end{aligned}$$

- Optimal design, physics simulation
- Inverse kinematics, inverse dynamics
- Model predictive control, reinforcement learning
- State observation, estimation (SLAM, etc.)

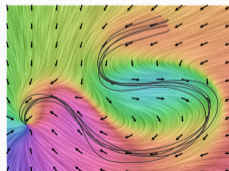
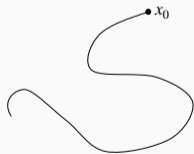
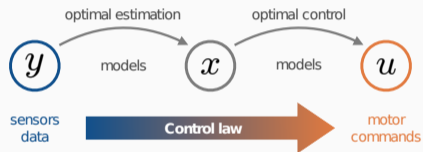
PERCEPTION-DECISION-ACTION LOOP



OPTIMAL CONTROL VS POLICY LEARNING

OPTIMAL CONTROL

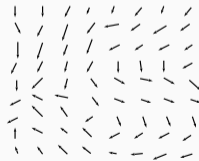
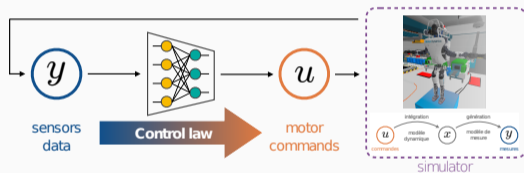
$$\min_{x(\cdot), u(\cdot)} \int_0^T l_t(x(t), u(t)) dt$$
$$\dot{x}(t) = f_t(x(t), u(t))$$
$$x(0) = x_0$$



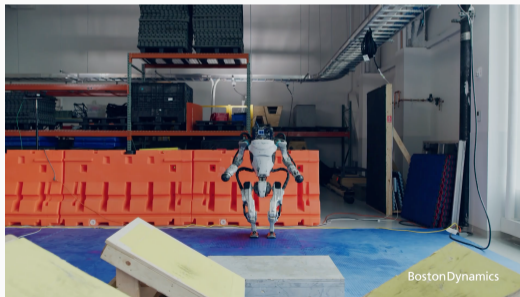
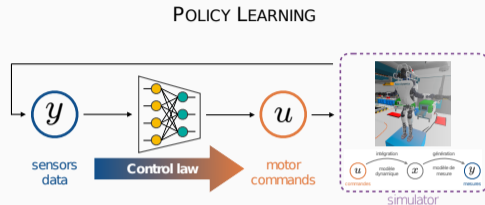
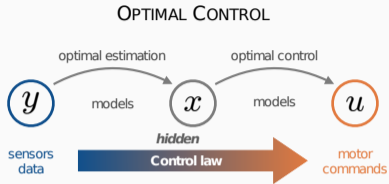
Source: Callinon et al.

POLICY LEARNING

$$\min_{\theta} \mathbb{E}_{\xi} \left[\int_0^T l_t(x(t), \pi_{\theta}(x(t), \xi(t))) dt \right]$$
$$\dot{x}(t) = f_t(x(t), \pi_{\theta}(x_t, \xi_t))$$
$$x(0) \sim \xi_0$$



OPTIMAL CONTROL VS POLICY LEARNING: ROBOTS





Robotics @ WILLOW

Perception, Learning and Control

Faculties:

- * [Ivan Laptev](#) (Inria, 100%)
- * [Justin Carpentier](#) (Inria, 100%)
- * [Jean Ponce](#) (Inria, 100%)
- * [Cordelia Schmid](#) (Inria, 50%)
- * [Stéphane Caron](#) (Inria, 100%)

External collaborators:

- * [Josef Sivic](#) (CTU)

Post-docs:

- * Shizhe Chen
- * Alexandre Araujo

Engineers:

- * [Etienne Arlaud](#) (Inria, SED-Paris)
- * [Pierre-Guillaume Raverdy](#) (Inria, SED-Paris)

Visitors:

- * [Kateryna Zorina](#) (CTU Prague)

Assistant:

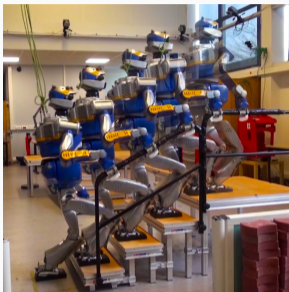
- * Julien Guieu

PhD students:

- * [Yann Labbé](#)
- * [Antoine Bambade](#)
- * [Robin Strudel](#)
- * [Zongmian Li](#)
- * Bruno Lecouat
- * [Yann De Mont Marin](#)
- * [Pierre-Louis Guhur](#)
- * [Oumayma Bounou](#)
- * [Elliot Chane-Sane](#)
- * Antoine Yang
- * [Quentin Le Lidec](#)
- * Guillaume Le Moing
- * Hugo Cisneros
- * Alaaeldin El-Nouby
- * [Thomas Chabal](#)
- * Adrien Bardes
- * [Wilson Jallet](#)
- * Nicolas Chahine
- * Elliot Vincent
- * Théo Bodrito
- * Matthieu Futral-Peter
- * Zerui Chen
- * [Fabian Schramm](#)

- **Optimization:** numerical solvers for robotics (AB, WJ)
- **Simulation:** contact simulation and non-smooth differentiation (QLL, LM)
- **Perception:** object pose estimation, world representations (YL)
- **Control:** model predictive control for manipulation and locomotion (WJ)
- **Learning:** reinforcement learning, interplay with optimal control (FS)

OPTIMIZATION PLAYS A KEY ROLE IN ROBOTICS



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- Optimal design, physics simulation
- **Inverse kinematics**, inverse dynamics
- Model predictive control, **reinforcement learning**
- State observation, estimation (SLAM, etc.)

INVERSE KINEMATICS

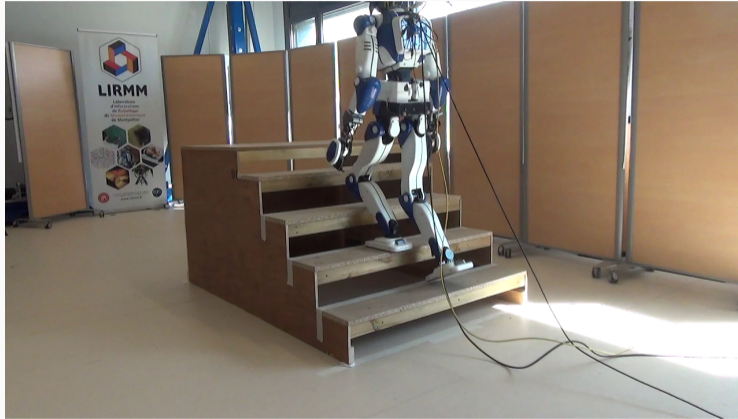
Make a robot **move** (motion) to achieve some **tasks** (control).

Examples:

- Locomotion: change position w.r.t. the world
- Manipulation: change the pose of an object w.r.t. the robot
- Folding: change the configuration of a deformable object
- Breaking: add free-flyer joint to another system ;)

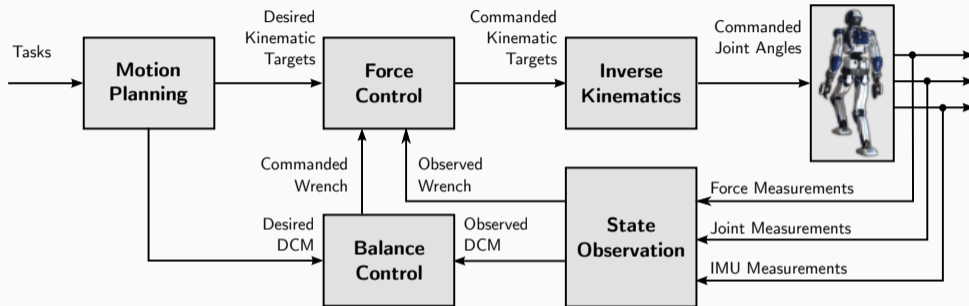
Key part of the work: task formulation.

STAIR CLIMBING



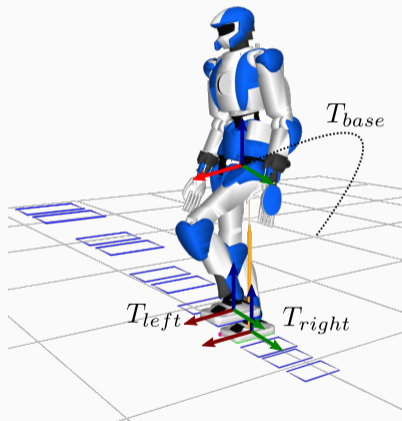
Video: <https://www.youtube.com/watch?v=vFCFKAunsYM>

CONTROLLER PIPELINE



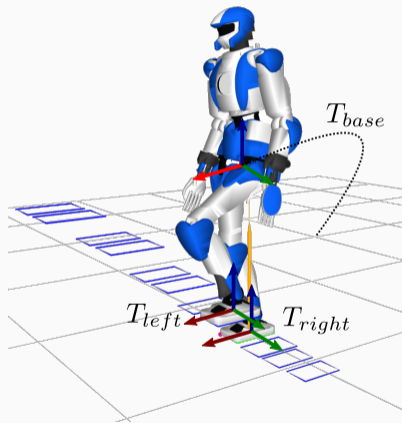
²Stéphane Caron, Abderrahmane Kheddar, and Olivier Tempier. "Stair Climbing Stabilization of the HRP-4 Humanoid Robot using Whole-body Admittance Control". In: *IEEE International Conference on Robotics and Automation*. May 2019.

- **Goal:** move to fulfill a set of tasks
- **Configuration space:** $q \in \mathcal{C}$ is a manifold
- **Joints:** q_i in sub-manifolds, e.g. $q_i \in SO(2)$
- **Foot task:** move ${}^0T_{foot}(q) \in SE(3)$ to ${}^0T_{foot*}$
- **Error:** $e_i(q) = \log_6({}_{foot}T_{foot*}(q))$
 - Goal: $\forall i, e_i(q) \rightarrow 0$
- **Jacobian:** $J_i(q) = \nabla_q e_i(q)$
- **Dynamics:** $\dot{e}_i(q) = J_i(q)v = -\alpha e_i(q)$
 - No constraint $\Rightarrow e_i(q) \rightarrow 0$ exponentially
- **Constraints:** $q \in \mathcal{C}_{free} \subset \mathcal{C}$
- **Multi-tasks:** weighted/lexicographic optim.



$$\begin{aligned} & \underset{v}{\text{minimize}} && \sum_i \|J_i(q)v + \alpha e_i(q)\|_{W_i}^2 \\ & \text{subject to} && G(q)v \leq h(q) \\ & && A(q)v = b(q) \end{aligned}$$

- Gauss-Newton approximation
- Velocity v is **both** the step and motor command: moving is thinking
- No line search!
- Levenberg-Marquardt damping, but numerical instability when $J_i(q)$ singular



$$\begin{aligned} & \underset{x}{\text{minimize}} && \frac{1}{2}x^T P x + q^T x \\ & \text{subject to} && Gx \leq h \\ & && Ax = b \end{aligned}$$

```

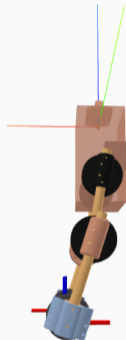
from qpsolvers import solve_qp

M = np.array([[1., 2., 0.], [-8., 3., 2.], [0., 1., 1.]])
P = M.T @ M # this is a positive definite matrix
q = np.array([3., 2., 3.]) @ M
G = np.array([[1., 2., 1.], [2., 0., 1.], [-1., 2., -1.]])
h = np.array([3., 2., -2.])
x = solve_qp(P, q, G, h, solver="proxqp")
    
```

Setup: `pip install proxsuite qpsolvers`

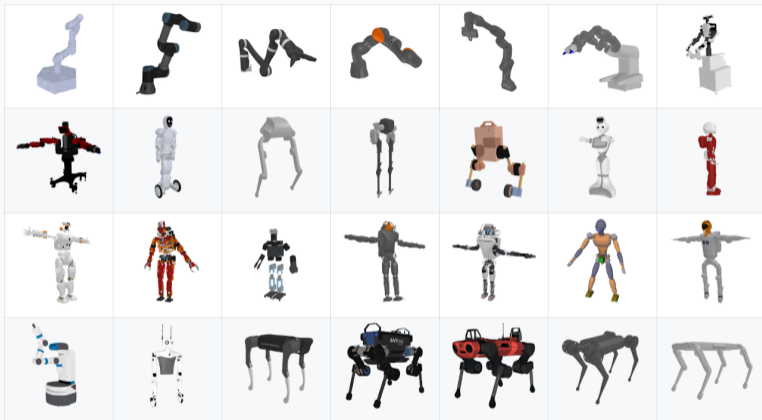
```
from pink import solve_ik
from loop_rate_limiters import RateLimiter

rate = RateLimiter(frequency=200)
dt = rate.period
for t in np.arange(0., 42., dt):
    update_targets(tasks, t, dt)
    v = solve_ik(q, tasks, dt, solver="proxqp")
    q.integrate(v, dt)
    rate.sleep()
```



Setup: `pip install loop-rate-limiters proxsuite pin-pink`

REALLY, ANY ROBOT

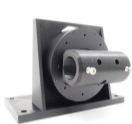


```
List: pip install robot_descriptions
```

REINFORCEMENT LEARNING

Data!





qdd100 beta 2 developer kit
\$499.00



qdd100 beta 2 servo
\$439.00



moteus r4.11 developer kit
\$214.00



mjbots pi3hat r4.4b
from \$149.00



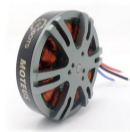
mjbots power dist r4.3b
\$139.00



fdcanusb
\$109.00



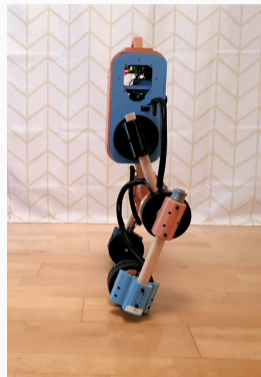
moteus r4.11 controller
\$104.00



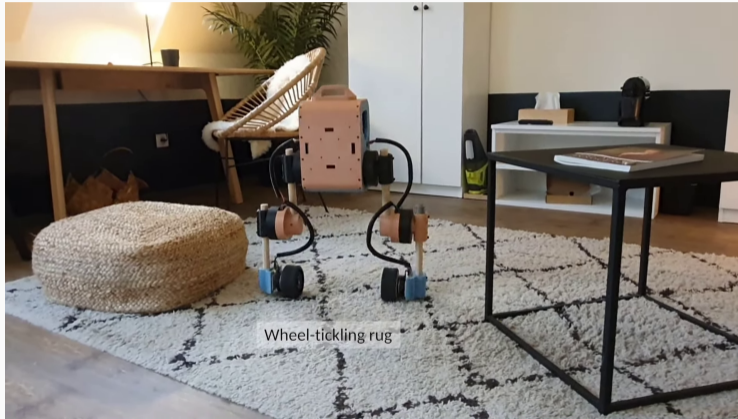
mj5208 brushless motor
\$60.00

Wheeled biped:

- Joints: 6 (hips, knees, wheels)
- Total mass: 5.4 kg
- Computer: Raspberry Pi
- Print time: ≤ 100 h
- Actuators + electronics: 3,000 €
- **Autonomy:** 3–4 h with 5.0 Ah battery
- Sensors: IMU, joint position, velocity, torque
- Extensibility: 12 actuators, external sensors



<https://hackaday.io/project/185729-upkie-homemade-wheeled-biped-robot>

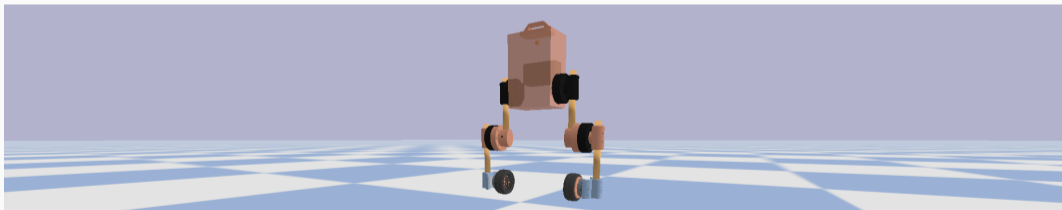


Video: https://www.youtube.com/watch?v=NO_TkHGS0wQ

Software that comes batteries included:

```
git clone https://github.com/tasts-robots/upkie_locomotion.git
cd upkie_locomotion
./tools/bazelisk run -c opt //agents/ppo_balancer:train
```

Bazel will download and build everything (no installation required on Linux).



Repository: https://github.com/tasts-robots/upkie_locomotion

```
import gym
import upkie_locomotion.envs

upkie_locomotion.envs.register()
env = gym.make("UpkieWheelsEnv-v1") # same for sim or real robot
observation = env.reset(seed=42)
action = 0.0 * env.action_space.sample()
for step in range(1_000_000):
    observation, reward, done, _ = env.step(action)
    if done:
        observation = env.reset()
        pitch = observation[0]
        action[0] = 10.0 * pitch
env.close()
```

Setup: `pip install upkie_locomotion`

WORLD REPRESENTATIONS?

ANOTHER SOURCE OF DATA



1. **Optimization** plays a key role in robotics
 - Come test your algorithms!
2. Building robots has become 10x **cheaper**
 - Come get relevant problems and data!
3. **Open source** hardware and software
 - Just `pip install`, no strings attached

THANK YOU FOR YOUR ATTENTION!



Bibliography

- [CKT19] Stéphane Caron, Abderrahmane Kheddar, and Olivier Tempier. “Stair Climbing Stabilization of the HRP-4 Humanoid Robot using Whole-body Admittance Control”. In: *IEEE International Conference on Robotics and Automation*. May 2019.
- [Tod18] Emanuel Todorov. “Goal directed dynamics”. In: *IEEE International Conference on Robotics and Automation*. 2018.